

# Math 115

## Spring 2017

### Lecture 8

Find two consecutive odd integers such that  
5 times the smaller one reduced by the larger  
one is equal to 90.

Smaller  $x$

Larger  $x+2$

$$5 \cdot \text{Smaller} - \text{larger} = 90$$

$$5 \cdot x - (x+2) = 90$$

$$5x - x - 2 = 90$$

$$4x = 92$$

$$x = 23$$

23 & 25

Find two consecutive even integers such that 7 times the first one is equal to the difference of 370 and the second one.

$$7 \cdot \text{First} = 370 - \text{Second}$$

$$\begin{aligned} \text{First} &\rightarrow x \\ \text{Second} &\rightarrow x+2 \end{aligned}$$

$$7 \cdot x = 370 - (x+2)$$

$$7x = 370 - x - 2$$

$$7x + x = 368$$

$$8x = 368$$

$$x = 46$$

$$46 \text{ \& } 48$$

Find three consecutive integers such that the sum of the first one and 3 times the third one is equal to 350 less twice the second.

$$\text{First} + 3 \cdot \text{Third} = 350 - 2 \cdot \text{Second}$$

$$\text{First} \rightarrow x$$

$$\text{Second} \rightarrow x+1$$

$$\text{Third} \rightarrow x+2$$

$$A \text{ less } B \rightarrow A - B$$

$$\begin{aligned} A \text{ less than } B \\ \rightarrow B - A \end{aligned}$$

$$x + 3(x+2) = 350 - 2(x+1)$$

$$x + 3x + 6 = 350 - 2x - 2$$

$$4x + 2x = 348 - 6$$

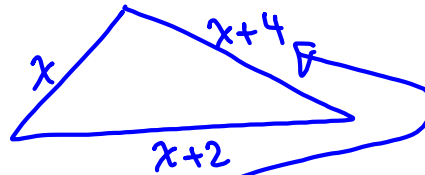
$$6x = 342 \rightarrow x = 57$$

$$57, 58, \text{ \& } 59$$

The perimeter of a triangle is 231 inches.

Three sides are three cons. odd integers.

① Draw & label



② Set-up the eqn & Solve

③ Give the largest side.

$$75 + 4 = 79$$

79 inches

$$P = 231$$

$$a + b + c = 231$$

$$x + x + 2 + x + 4 = 231$$

$$3x + 6 = 231$$

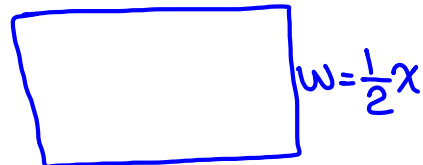
$$3x = 225$$

$$\boxed{x = 75}$$

A rectangular room has a perimeter of 72 ft.

the width is half its length.

① Draw & label.



② Set-up the eqn & Solve.

$$L = x$$

$$P = 72$$

③ Give its dimensions.

24 ft by 12 ft

$$2L + 2W = 72$$

$$2x + 2\left(\frac{1}{2}x\right) = 72$$

$$2x + x = 72$$

$$3x = 72$$

$$\boxed{x = 24}$$

④ Give its area.

$$A = LW$$

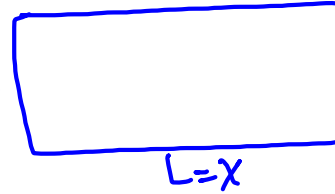
$$= 24 \cdot 12$$

$$\boxed{A = 288 \text{ ft}^2}$$

The width of a rectangular room is 3m shorter than half its length.  
Perimeter of the room is 102 m. Find its area

① Draw & label

$$w = \frac{1}{2}x - 3$$



② Set-up the eqn & Solve

③ look for area

$$\text{Length} = 36\text{m}$$

$$\text{width} = \frac{1}{2}(36) - 3 = 18 - 3 = 15\text{m}$$

$$A = LW = 36(15) = \boxed{540\text{m}^2}$$

$$P = 102$$

$$2L + 2W = 102$$

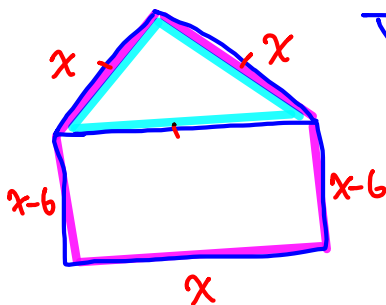
$$2x + 2\left(\frac{1}{2}x - 3\right) = 102$$

$$2x + x - 6 = 102$$

$$3x = 108$$

$$x = 36$$

An equilateral triangle is on top of the length of a rectangle as shown below:



The width of the rectangle is 6 inches shorter than its length.

The perimeter of the shape is 68 inches. Find the perimeter of the triangle.

$$\boxed{x} + \boxed{x-6} + \boxed{x} + \boxed{x} + \boxed{x-6} = 68$$

$$5x - 12 = 68$$

$$5x = 80$$

$$\boxed{x = 16}$$

$$P_{\text{Triangle}} = 3x$$

$$P = 3(16) = \boxed{48\text{ inches}}$$

Every 1.5 inches on the map is for 175 miles actual distance.

Two cities are 12 inches apart on a map.  
Find actual distance by using ratio & Proportion.

$$\frac{1.5 \text{ inches}}{175 \text{ miles}} = \frac{12 \text{ inches}}{x \text{ Miles}}$$

1400 miles

Solve

$$\frac{1.5}{175} = \frac{12}{x}$$

$$1.5x = 12(175)$$

$$x = \frac{12(175)}{1.5}$$

$$x = 1400$$

Use two methods to solve:

What percent of 880 is 92.4?

$$\frac{P}{100} \cdot 880 = 92.4$$

$$8.8P = 92.4$$

$$P = \frac{92.4}{8.8}$$

$$P = 10.5$$

10.5%

$$\frac{P}{100} = \frac{\text{Part}}{\text{whole}}$$

$$\frac{P}{100} = \frac{92.4}{880}$$

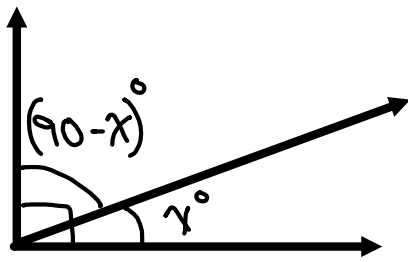
$$880P = 100(92.4)$$

$$P = \frac{100(92.4)}{880}$$

$$P = 10.5$$

10.5%

Two angles are called Complementary angles if their sum is  $90^\circ$



$$20^\circ \text{ \& \; } 70^\circ$$

$$40^\circ \text{ \& \; } 50^\circ$$

$$68^\circ \text{ \& \; } 22^\circ$$

$$1^\circ \text{ \& \; } 89^\circ$$

Find two complementary angles

Such that the sum of twice the first and  
3 times the second is 200.

First  $\rightarrow x$

Second  $\rightarrow 90-x$

$$2 \cdot \text{First} + 3 \cdot \text{Second} = 200$$

$$2 \cdot x + 3(90 - x) = 200$$

$$\underline{\underline{2x}} + \underline{\underline{270}} - \underline{\underline{3x}} = 200$$

$$-x = 200 - 270$$

$$-x = -70 \rightarrow x = 70$$

$$70^\circ \text{ \& \; } 20^\circ$$

Find two complementary angles such that 4 times one of them is equal to 5 times the other one.

$$4x = 5(90 - x)$$

$$4x = 450 - 5x$$

$$4x + 5x = 450$$

$$9x = 450$$

$$x = 50$$

$$x \text{ \& } 90 - x$$

$$50^\circ \text{ \& } 40^\circ$$

Find two complementary angles such that the difference of 3 times one of them and 6 times the other one is equal to 0.

$$x \text{ \& } 90 - x$$

$$3x - 6(90 - x) = 0$$

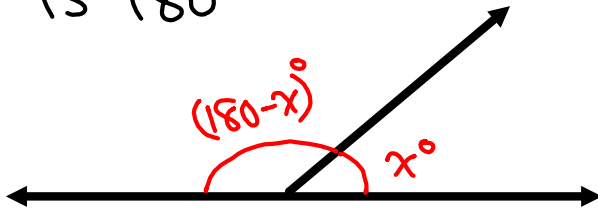
$$3x - 540 + 6x = 0$$

$$9x = 540$$

$$x = 60$$

$$60^\circ \text{ \& } 30^\circ$$

Two angles are Supplementary if their Sum is  $180^\circ$



$$10^\circ \text{ \& } 170^\circ$$

$$100^\circ \text{ \& } 80^\circ$$

$$30^\circ \text{ \& } 150^\circ$$

$$1^\circ \text{ \& } 179^\circ$$

Find two Supplementary angles

Such that the sum of 5 times one of them and 3 times the other one is 564.

$$5 \cdot x + 3 \cdot (180 - x) = 564$$

$$5x + 540 - 3x = 564$$

$$x \text{ \& } 180 - x$$

$$2x = 24$$

$$x = 12$$

$$12^\circ \text{ \& } 168^\circ$$

Find two Supplementary angles Such that 5 times one of them is equal to the sum of 260 and 3 times the other one.

$$5 \cdot x = 260 + 3(180 - x)$$

$$5x = 260 + 540 - 3x$$

$$5x + 3x = 800$$

$$8x = 800$$

$$x = 100$$

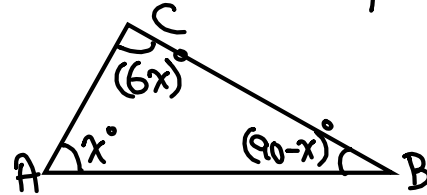
$$x \text{ \& } 180 - x$$

$$100^\circ \text{ \& } 80^\circ$$



In triangle ABC, Angles A and B are Complementary. Angle C is 6 times angle A.

① Draw & label.



② Set up your eqn. & solve

$$A + B + C = 180$$

$$\cancel{x} + 90 - \cancel{x} + 6x = 180$$

$$6x = 90$$

$$x = 15$$

③ Find all three angles.

$$m\angle A = 15^\circ$$

$$m\angle B = 75^\circ$$

$$m\angle C = 90^\circ$$

### Agenda for Tuesday

1) Collect SG 6 & 7 at 6:00 AM

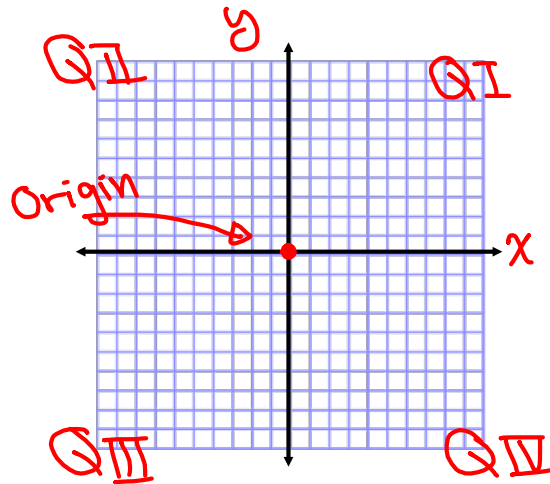
2) Turn in any work that you, for whatever reason, did not turn in. for some credit.  
at 6:00 AM

3) lecture

4) Exam 1 starts around 7:20.

Introduction to graphing:

Points  $\rightarrow (x, y)$        $(3, 2), (-4, 7),$   
 ordered-Pair       $(-2, -5), (0, -2),$   
                           $(8, -3), (4, 0),$   
                           $(0, 0)$



Rectangular  
Coordinate  
System

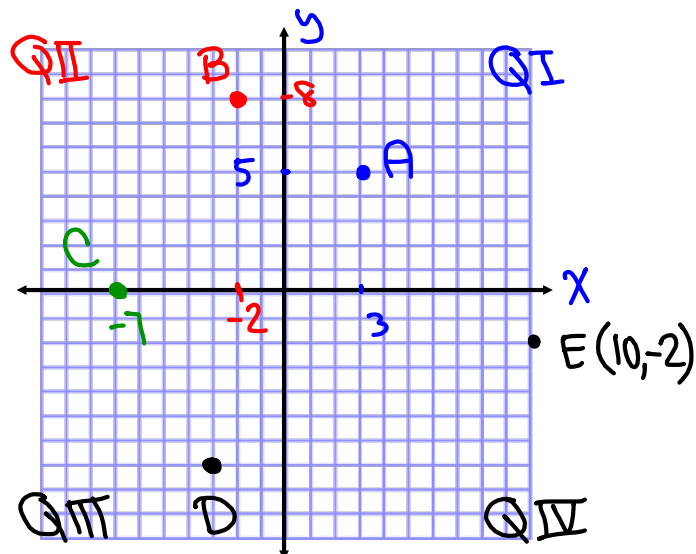
Plot

$A(3, 5)$

$B(-2, 8)$

$C(-7, 0)$

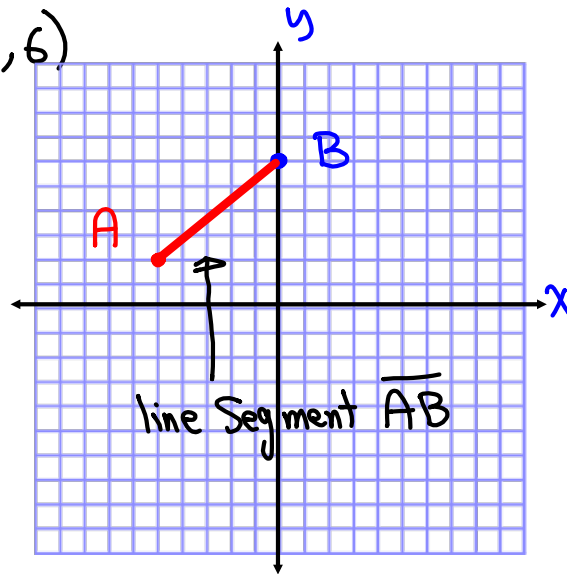
$D(-3, -7)$



$A(-5, 2)$  &  $B(0, 6)$

Plot  $A$  &  $B$ ,

Connect  $A$  to  $B$   
by a straight line



$A(-4, 0)$  ,  $B(7, -3)$

① Plot  $A$  &  $B$

② Draw  $\overline{AB}$

